Name:

Math 254 Fall 2014 Exam 4

Please read the following directions:
Please print your name in the space provided, using large letters, as "First LAST". Books, notes, calculators, and other aids are not permitted on this exam. Please write legibly, with plenty of white space. Please put your answers in the designated areas. Show all necessary work in your solutions; if you are unsure, show it. Cross out work you do not wish graded; incorrect work can lower your grade. All problems are worth 5-10 points; your total will be scaled to the standard 100 point scale. You have approximately 30 minutes.

Extra credit may be earned by handing in revised work in class on Wednesday 10/8; for details see the syllabus. You will find this exam on the instructor's webpage later today.

1. Carefully state the definition of "span". What type of object is it? Choose one from: [vector, scalar, vector space, list of numbers, set of numbers, linear combination, other]

2. Carefully state five of the eight vector space axioms.

The remaining three problems concern the vector space $V = \mathbb{R}^4$ and the subsets
$S = \{(a, b, c, d) : a + b = c + d = 0\}$, $T = \{(a, b, c, d) : a + c = d = 0\}$.

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3. Prove that S is a subspace of V.

4. Prove that $S \cap T = \{0\}$. (you may assume that S, T are vector spaces)

5. Prove that each of the four standard basis vectors e_1, e_2, e_3, e_4 are in $S + T$.